

## CE141 Example Questions

### Question 1

Which of the following is not a proposition?

- [A] All CE141 lectures take place in LTB7
- [B] Is London East of Colchester?
- [C] Colchester is the capital of the United Kingdom
- [D] All cows eat grass

### Question 2

Which of the following strings, involving propositions  $p$ ,  $q$  and  $r$ , is a valid logical expression?

- [A]  $\vee (p \wedge q) \vee r$
- [B]  $(p \wedge)q \wedge r$
- [C]  $p \vee (q \wedge \neg r)$
- [D]  $p \neg \wedge q$

### Question 3

The truth table for the compound proposition  $\neg p \wedge q$  is:

[A]

$p$	$q$	$\neg p \wedge q$
F	F	F
F	T	F
T	F	T
T	T	F

[B]

$p$	$q$	$\neg p \wedge q$
F	F	F
F	T	T
T	F	F
T	T	F

[C]

$p$	$q$	$\neg p \wedge q$
F	F	T
F	T	T
T	F	F
T	T	T

[D]

$p$	$q$	$\neg p \wedge q$
F	F	T
F	T	F
T	F	T
T	T	T

**Question 4**

Which of the following partially completed truth tables is correct for the compound proposition  $(p \wedge q) \vee r$ ?

[A]

$p$	$q$	$r$	$(p \wedge q) \vee r$
F	F	F	T
$\vdots$	$\vdots$	$\vdots$	$\vdots$

[B]

$p$	$q$	$r$	$(p \wedge q) \vee r$
$\vdots$	$\vdots$	$\vdots$	$\vdots$
F	T	F	T
$\vdots$	$\vdots$	$\vdots$	$\vdots$

[C]

$p$	$q$	$r$	$(p \wedge q) \vee r$
$\vdots$	$\vdots$	$\vdots$	$\vdots$
T	T	F	T
$\vdots$	$\vdots$	$\vdots$	$\vdots$

[D]

$p$	$q$	$r$	$(p \wedge q) \vee r$
$\vdots$	$\vdots$	$\vdots$	$\vdots$
F	T	T	F
$\vdots$	$\vdots$	$\vdots$	$\vdots$

**Question 5**

Consider the following propositions:

$p$  := “John speaks English”

$q$  := “John speaks French”

$r$  := “Jane speaks English”

$s$  := “Jane speaks French”

Neither John nor Jane speaks any other language. Which of the following is the most appropriate logical expression to represent the proposition: “John and Jane are able to communicate”?

[A]  $(p \vee q) \wedge (r \vee s)$

[B]  $(p \wedge q) \vee (r \wedge s)$

[C]  $(p \vee r) \wedge (q \vee s)$

[D]  $(p \wedge r) \vee (q \wedge s)$

**Question 6**

Which of the following compound propositions is equivalent to  $\neg p \wedge \neg q$ ?

[A]  $\neg(p \wedge q)$

[B]  $\neg p \wedge \neg q$

[C]  $\neg(p \vee q)$

[D]  $p \wedge q$

**Question 7**

Which of the following is not a valid identity?

- [A]  $p \vee q \equiv q \vee p$   
 [B]  $(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$   
 [C]  $(p \vee q) \vee \neg r \equiv p \vee \neg(q \vee r)$   
 [D]  $p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$

**Question 8**

The truth table for the *conditional* proposition  $p \rightarrow q$  is:

- |       |     |     |  |                   |
|-------|-----|-----|--|-------------------|
| [A]   | $p$ | $q$ |  | $p \rightarrow q$ |
| ----- |     |     |  |                   |
|       | F   | F   |  | F                 |
|       | F   | T   |  | T                 |
|       | T   | F   |  | T                 |
|       | T   | T   |  | F                 |
- |       |     |     |  |                   |
|-------|-----|-----|--|-------------------|
| [B]   | $p$ | $q$ |  | $p \rightarrow q$ |
| ----- |     |     |  |                   |
|       | F   | F   |  | T                 |
|       | F   | T   |  | F                 |
|       | T   | F   |  | F                 |
|       | T   | T   |  | T                 |
- 
- |       |     |     |  |                   |
|-------|-----|-----|--|-------------------|
| [C]   | $p$ | $q$ |  | $p \rightarrow q$ |
| ----- |     |     |  |                   |
|       | F   | F   |  | T                 |
|       | F   | T   |  | T                 |
|       | T   | F   |  | F                 |
|       | T   | T   |  | T                 |
- |       |     |     |  |                   |
|-------|-----|-----|--|-------------------|
| [D]   | $p$ | $q$ |  | $p \rightarrow q$ |
| ----- |     |     |  |                   |
|       | F   | F   |  | T                 |
|       | F   | T   |  | F                 |
|       | T   | F   |  | T                 |
|       | T   | T   |  | T                 |

**Question 9**

Which of the following logical expressions is a tautology?

- [A]  $(p \wedge q) \vee T$   
 [B]  $(p \wedge q) \vee F$   
 [C]  $(p \vee q) \wedge T$   
 [D]  $(p \vee q) \wedge F$

**Question 10**

Which of the following logical expressions is a contradiction?

- [A]  $(p \wedge q) \vee T$   
 [B]  $(p \wedge q) \vee F$   
 [C]  $(p \vee q) \wedge T$   
 [D]  $(p \vee q) \wedge F$